



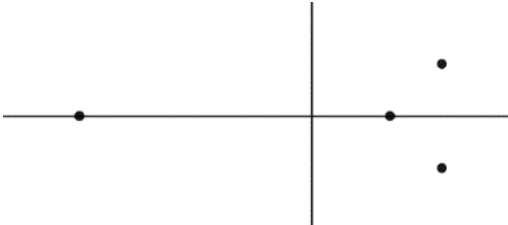
Mark Scheme (Results)

Summer 2024

Pearson Edexcel International Advanced Level
In Further Pure Mathematics (WFM01) Paper 01

Question Number	Scheme	Notes	Marks
1(i)	$\mathbf{A} = \begin{pmatrix} 3k & 4k-1 \\ 2 & 6 \end{pmatrix}$		
(a)	$3k \times 6 - 2(4k-1) = 0 \Rightarrow k = \dots$ Forms $\det \mathbf{A} = 0$ and solves for k . The “= 0” can be implied by a solution for k . Award for $3k \times 6 - 2(4k-1) = 0 \Rightarrow k = \dots$ If LHS is only seen expanded 2 terms of $18k - 8k + 2$ must be correct (implied by $10k$) May use $ad = bc$ and condone $\det \mathbf{A} = bc - ad = 0$ but clear use of $ad + bc$ is M0		M1
	$(10k + 2 = 0 \Rightarrow k =) -\frac{1}{5}$ or -0.2	A1: Correct value. Accept $-\frac{2}{10}$	A1
(2)			
(b)	$(\mathbf{A}^{-1} =) \frac{1}{10k+2} \begin{pmatrix} 6 & 1-4k \\ -2 & 3k \end{pmatrix} \text{ or } \begin{pmatrix} \frac{6}{10k+2} & \frac{1-4k}{10k+2} \\ -2 & 3k \end{pmatrix} \text{ or e.g., } \begin{pmatrix} \frac{3}{5k+1} & \frac{1-4k}{10k+2} \\ -1 & 3k \end{pmatrix}$ M1: for $\dots \begin{pmatrix} 6 & 1-4k \\ -2 & 3k \end{pmatrix}$ Ignore any multiplier and accept without one and condone if this matrix is labelled as \mathbf{A}^{-1} . Allow unsimplified e.g., $\dots \begin{pmatrix} 6 & -(4k-1) \\ -2 & 3k \end{pmatrix}$ Allow if determinant incorporated provided it is clear that the elements of $\text{Adj}(\mathbf{A})$ are correct A1ft: $\frac{1}{10k+2} \begin{pmatrix} 6 & 1-4k \\ -2 & 3k \end{pmatrix}$ Fully correct inverse ft their determinant in form $ak + b$ $a, b \neq 0$ and simplified but if determinant incorporated there is no requirement to write e.g., $\frac{6}{10k+2}$ as $\frac{3}{5k+1}$. Allow different brackets e.g., [...], {...} but $ \dots $ is M0 if followed by an attempt at $\det(\text{Adj}(\mathbf{A}))$. Allow if “ \times ” is between fraction and matrix and allow fraction to appear on the right of the matrix. Isw when a correct answer is seen but this mark is not available if they substitute a value of k into the determinant and/or matrix.		M1 A1ft
(2)			
(ii)(a)	$p = q = -2$ or $(\mathbf{B} =) \begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix}$	Both values identified or correct matrix (any or no bracket). Allow “Both are -2” or “-2, -2”	B1
(b)	$p = -1 \quad q = 1$ or $(\mathbf{B} =) \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	Both values identified or correct matrix (any or no bracket). Allow “-1, +1” (Mark in order presented). No trig expressions.	B1
(2)			
Total 6			

Question Number	Scheme	Notes	Marks
2	$f(z) = z^3 - 13z^2 + 59z + p$		
(a)	$[f(3) =]3^3 - 13(3)^2 + 59(3) + p$ <p>or e.g., $27 - 117 + 177 + p$ or</p> $z - 3 \overline{) \begin{array}{r} z^3 - 13z^2 + 59z + p \\ \underline{z^3 - 3z^2} \\ -10z^2 + 59z \\ \underline{-10z^2 + 30z} \\ 29z + p \\ \underline{29z - 87} \\ 0 \end{array}}$	<p>Attempts $f(3)$.</p> <p>Must see more than just $87 + p$</p> <p>Allow one slip (e.g., a miscopy of one coefficient, or one incorrect value/sign if expression just given as $27 - 117 + 177 + p$)</p> <p>Alternatively long divides by $z - 3$ obtaining a 3TQ with two terms of $z^2 - 10z + 29$ correct.</p> <p>Could use synthetic division. An attempt at equating coefficients/factorising requires 2 correct values for the a, b and c of $az^2 + bz + c$</p>	M1
	$f(3) = 0 \Rightarrow p = -87 *$	<p>Obtains "$p = -87$" only with no errors but condone work in x</p> <p>"=0" must have been seen before $p = -87$ if $f(3)$ attempted but allow just $p = -87$ following a full and correct attempt via division/equating coefficients etc with no errors.</p>	A1* (shown as B1 on ePen)
(2)			
(b)	<p>Allow equivalent work in x. Allow use of a calculator to solve a quadratic. Solutions that just follow $z^3 - 13z^2 + 59z - 87 = 0$ score no marks. There are no marks if $z^2 - 10z + 29$ has clearly been produced by using $(z - (5 + 2i))(z - (5 - 2i))$</p>		
	$(z^3 - 13z^2 + 59z - 87) \div (z - 3)$ $= \dots [z^2 - 10z + 29]$	<p>M1: Uses $z \pm 3$ with $f(z)$ (not their $f(z)$) to obtain a 3TQ expression with evidence of any appropriate method including inspection (must be evidence of use of $z \pm 3$) or equating coefficients. Ignore any remainder if long division is used and may see $z^2 - 16z + 107$ ($r(-408)$) if $z + 3$ used. Must be seen or referred to in (b)</p> <p>A1: Correct quadratic</p>	M1 A1
	$z = \frac{-(-10) \pm \sqrt{(-10)^2 - (4)(1)(29)}}{2(1)}$ <p>or</p> $(z - 5)^2 - 25 + 29 = 0 \Rightarrow z = 5 \pm \sqrt{-4}$	<p>Solves their 3TQ arising from using $(z - 3)$ only as a factor (usual rules but allow if one correct root if calculator used on their quadratic)</p> <p>If a sum/product of roots method is used on their 3TQ (i.e., $2a = -(-10)$, $a^2 + b^2 = "29"$) it must be complete and condone only sign errors. Do not allow just $5 \pm 2i$ following an incorrect quadratic</p> <p>Requires previous M mark.</p>	dM1
	$\left(z = \frac{10 \pm \sqrt{-16}}{2} = \right) 5 \pm 2i$	$5 \pm 2i$ or $5 + 2i, 5 - 2i$ only. Not $5 \pm 2\sqrt{-1}$ Accept $\pm 2i + 5$	A1
(4)			

Question Number	Scheme	Notes	Marks
2(c)	 <p>Look for this arrangement if correct but note potential ft</p>	<p>Correct diagram ft their $a \pm bi$ ($a, b \neq 0$)</p> <p>Diagram should be roughly symmetrical in the real axis. The point on the negative x-axis should be further from the origin than the point on the positive x-axis but ignore any other scaling issues – just look for the $a \pm bi$ points to be placed in the correct quadrants, roughly aligned vertically and placed correctly relative to the given point that is on the same side of the y-axis.</p> <p>Points/axes may be unlabelled or mislabelled. If vectors/lines are used the end points must satisfy the conditions above.</p>	B1ft
			(1)
(d)	$2\left(\sqrt{("5"-(-9))^2 + "2"^2} + \sqrt{("5"-3)^2 + "2"^2}\right)$	<p>A correct numerical expression for the perimeter ft their $a \neq 0$ or 3 or -9 and $b \neq 0$</p> <p>This mark requires working with points that would form a convex or concave kite where the x-axis is a line of symmetry.</p> <p>Working must be seen if $a \pm bi$ incorrect but allow just $4\sqrt{5} + 4\sqrt{17}$ oe from using $-5 \pm 2i$</p>	M1
	$\left[= 2\left(\sqrt{14^2 + 2^2} + \sqrt{2^2 + 2^2}\right) = 2\left(\sqrt{200} + \sqrt{8}\right) \right]$ $= 24\sqrt{2}$	<p>$24\sqrt{2}$ or any simplified equivalent e.g., $12\sqrt{8}$ or $2\sqrt{288}$ but not $\sqrt{1152}$. Correct answer scores both marks and allow M1 A0 for just $\sqrt{1152}$</p>	A1
(2)			
Total 9			

Question Number	Scheme	Notes	Marks
3	$f(x) = x^3 - 5\sqrt{x} - 4x + 7$		
(a)	$f(0.25)=3.515625, \frac{225}{64}, 3\frac{33}{64} \quad f(1) = -1$	Attempts both $f(0.25)$ and $f(1)$ with one correct allowing awrt 3.52 for $f(0.25)$	M1
	<p>examples: “1” refers to “-1” with sign corrected</p> $\frac{\alpha - 0.25}{\text{"3.515625"}} = \frac{1 - \alpha}{\text{"1"}} \Rightarrow \alpha = \dots$ $\frac{\alpha - 0.25}{\text{"}\frac{225}{64}\text{"}} = \frac{1 - \alpha}{\text{"1"}} \Rightarrow \alpha = \dots$ $\frac{\alpha - 0.25}{\text{"3.515625"}} = \frac{1 - 0.25}{\text{"3.515625"} + \text{"1"}} \Rightarrow \alpha = \dots$ $\frac{1 - \alpha}{\text{"1"}} = \frac{1 - 0.25}{\text{"3.515625"} + \text{"1"}} \Rightarrow \alpha = \dots$ <p>$[\alpha - 0.25 = 3.515625 - 3.515625\alpha$ $4.515625\alpha = 3.765625]$</p>	<p>Forms an equation in α that is correct for their values and solves for α. Can use x etc. Allow e.g., “f(0.25)” and “-f(1)” in this equation provided values for these are seen. Any modulus signs must be applied and $f(0.25)$ and $f(1)$ must have had different signs.</p> <p>Can be implied by just awrt 0.83 or $\frac{241}{289}$ but otherwise a correct equation for their $f(0.25)$ and $f(1)$ must be seen but allow use of $\frac{af(b)-bf(a)}{f(b)-f(a)} \Rightarrow \frac{1(\text{"3.515625"})-0.25(\text{"-1"})}{\text{"3.515625"}-(\text{"-1"})}$ or a correct partially processed equivalent and only allow formula followed by value if values for $a, b, f(a)$ and $f(b)$ are seen</p> <p>If e.g., A is used for $\alpha - 0.25$ then must see $A + 0.25$ later. Note that sight of 1.2981... or $\frac{209}{161}$ usually indicates a sign error.</p>	M1
	$\alpha = 0.834$	awrt 0.834 (0.8339100346...) Must be decimal. Ignore labelling and just look for this value. [Note: actual root is 0.767843...]	A1
(3)			
Alt for last 2 marks (straight line equation)	<p>e.g., $y = \frac{\text{"3.515625"} - \text{"(-1)"}}{0.25 - 1}x + c$</p> <p>$(1, \text{"-1"}) \Rightarrow -1 = -6.0208\dot{3} + c$ $\Rightarrow c = 5.0208\dot{3}$</p> <p>$y = 0 \Rightarrow \alpha = \frac{-5.0208\dot{3}}{-6.0208\dot{3}} = 0.834$</p>	<p>M1: Any full method to find the equation of the line between (0.25, “3.515625”) and (1, “-1”) and then uses $y = 0$ to find a value for α. Condone errors finding c and α but the initial equation should be correct for their $f(0.25)$ and $f(1)$ and the x and y coordinates should always be correctly placed.</p> <p>A1: awrt 0.834</p>	M1 A1
(b)	$[f'(x) =] \quad 3x^2 - \frac{5}{2}x^{-\frac{1}{2}} - 4$	<p>M1: 2 correctly differentiated terms (this includes $7 \rightarrow 0$)</p> <p>Allow unsimplified e.g., $3 \times x^{3-1}$</p> <p>A1: Fully correct simplified derivative</p>	M1 A1
(2)			
(c)	$x_1 = 1.75 - \frac{1.75^3 - 5\sqrt{1.75} - 4(1.75) + 7}{3(1.75)^2 - 2.5(1.75)^{-0.5} - 4}$ $\left[= 1.75 - \frac{-1.255003278...}{3.297677635...} = 1.75 + 0.38057... \right]$	<p>Uses a correct Newton-Raphson formula with $x_0 = 1.75$ and their $f'(x)$ to obtain a numerical expression for x_1 but implied by awrt 2.13 (2.13057185).</p> <p>Working must be seen if x_1 is wrong – allow “$x_0 = 1.75, x_1 = x_0 - \frac{f(x_0)}{f'(x_0)} = \dots$” or $1.75 - \frac{f(1.75)}{f'(1.75)} = \dots$”</p>	M1
	$x_1 = 2.13057185... \Rightarrow \beta = 2.131$	awrt 2.131 (ignore labelling and just look for this value). Ignore further iterations. [Note: actual root is 2.011276...]	A1
(2)			
Total 7			

Question Number	Scheme	Notes	Marks
4	If z is restated incorrectly, e.g., " $z = 3 + 4i$ " is seen allow a maximum of M1dM1A0 B0M1A1M1A0		
(a)	$z^2 - 3 = (-3 + 4i)(-3 + 4i) - 3$ $= 9 - 24i - 16 - 3$ $= -10 - 24i$	Substitutes $z = -3 + 4i$ into $z^2 - 3$, expands and reaches $a + bi$ ($a, b \neq 0$) Implied by $-10 - 24i$ seen and condone misapplication of the modulus e.g., using $a + bi$ from $ -a - bi $	M1
	$ z^2 - 3 = \sqrt{10^2 + 24^2}$	Correct expression for modulus of their $a + bi$ ($a, b \neq 0$) Allow with no working for the modulus provided answer correct for their $a + bi$ Requires previous M mark.	dM1
	26	26 only from correct work. e.g., $ -10 + 24i = 26$ is A0 Answer only or without $-10 - 24i$ is no marks.	A1
(3)			
(b)	$(z = -3 + 4i \Rightarrow) \quad z^* = -3 - 4i$	Correct conjugate. Can be implied	B1
	$\frac{50}{z^*} = \frac{50}{-3 - 4i} \times \frac{-3 + 4i}{-3 + 4i} \left[= 50 \times \frac{-3 + 4i}{25} \right]$ or $\frac{1}{z^*} = \frac{1}{-3 - 4i} \times \frac{-3 + 4i}{-3 + 4i} \left[= \frac{-3 + 4i}{25} \right]$	A correct multiplier seen that would make the denominator real for $\frac{50}{z^*}$ or $\frac{1}{z^*}$ where $z^* = \pm 3 \pm 4i$ (except $-3 + 4i$). If the multiplier is not seen must see something better than $50 \times \frac{-3 + 4i}{25}$ or $\frac{-3 + 4i}{25}$ or $-6 + 8i$ e.g., $\frac{50}{z^*} = \frac{50(-3 + 4i)}{9 + 16}$	M1
	$\frac{50}{z^*} = 2(-3 + 4i) \quad \text{or} \quad 2z$	Obtains $2(-3 + 4i)$ or $2z$ Just $-6 + 8i$ is insufficient Allow $k = 2$ provided " $= kz$ " or " $= k(-3 + 4i)$ " is seen	A1
(3)			
Using Result	May see: $\frac{50}{-3 - 4i} = k(-3 + 4i) \Rightarrow \frac{50}{9 + 16} = k \Rightarrow k = 2$ B1: Correct z^* M1: $\frac{50}{9 + 16} = k$ or better after multiplication A1*: $k = 2$		
Alt Using $\frac{1}{z^*} = \frac{z}{ z ^2}$	$\frac{1}{z^*} = \frac{z}{ z ^2}$ oe e.g., $z^* z = z ^2$	States or uses $\frac{1}{z^*} = \frac{z}{ z ^2}$ oe	B1
	$\frac{c}{z^*} = \frac{cz}{ z ^2}, \quad z = \sqrt{3^2 + 4^2} = \dots$	Expresses $\frac{c}{z^*}$ as $\frac{cz}{ z ^2}$ and attempts $ z $ or $ z ^2$ where $c = 1$ or 50	M1
	$\frac{50}{z^*} = \frac{50z}{25} = 2z$	Correctly finds $2z$ Allow $k = 2$ provided " $= kz$ " or " $= k(-3 + 4i)$ " is seen	A1

Question Number	Scheme	Notes	Marks
4(c)	$\arctan\left(\pm\frac{4}{3}\right) = \pm 0.927... (53.13^\circ)$ <p>or $\arctan\left(\pm\frac{3}{4}\right) = \pm 0.643... (36.86^\circ)$</p> <p>May see equivalent trig in which case the hypotenuse should be correct</p>	<p>Finds a relevant angle which could be in degrees correct to 2sf so accept awrt ± 0.93 (53°) or ± 0.64 (37°)</p> <p>If neither value is seen allow implication from the work</p> <p>May see e.g., $\tan^{-1}\left(\pm\frac{8}{6}\right) = ...$</p> <p>M0 if $\arg 2z$ replaced with $2 \arg z$</p>	M1
	$\left[\theta = \pi - 0.927295... \quad \theta = \frac{\pi}{2} + 0.643501... \right]$ $\theta = 2.21$	<p>Final answer of awrt 2.21 – do not isw. (n.b. $\theta = 2.214297436...$)</p> <p>Final answer of e.g., "$\pi - 0.927$" is A0</p> <p>Answer only scores both marks.</p> <p>Answer only in degrees (awrt 127°) is M1A0</p>	A1
Note: allow access to both marks even if k in part (b) was incorrect			(2)
			Total 8

Question Number	Scheme	Notes	Marks
5	$5x^2 - 4x + 2 = 0$		
	Solutions that rely on solving the given quadratic/finding values for p and q are likely to score a maximum of 0010 11010 if the relevant work is seen		
(a)(i)	$\frac{1}{p} \times \frac{1}{q} \text{ or } \frac{1}{pq} = \frac{2}{5} \Rightarrow pq = \frac{5}{2}^*$	Shows product of roots = $\frac{2}{5}$ followed by $pq = \frac{5}{2}$ Minimum as shown. Allow e.g., $qp = 2.5$ Note that $\frac{1}{pq} = \frac{1}{\frac{2}{5}} \Rightarrow pq = \frac{5}{2}$ is B0 No clearly incorrect work/statements.	B1*
	May see: $\left(x - \frac{1}{p}\right)\left(x - \frac{1}{q}\right) = x^2 - \left(\frac{1}{p} + \frac{1}{q}\right)x + \frac{1}{pq} = x^2 - \frac{4}{5}x + \frac{2}{5} \Rightarrow \frac{1}{pq} = \frac{2}{5} \Rightarrow pq = \frac{5}{2}^*$ Must not be any clearly incorrect work/statements.		
	Assuming result: $pq = \frac{5}{2} \Rightarrow \frac{1}{p} \times \frac{1}{q} = \frac{2}{5}$ requires conclusion e.g., "Hence true"		
(a)(ii)	$\frac{1}{p} + \frac{1}{q} = -\frac{(-4)}{5}$	Uses sum of roots to achieve a correct equation in p and q	M1
May use work from (i)	$\frac{1}{p} + \frac{1}{q} = \frac{p+q}{pq}$	States or uses $\frac{1}{p} + \frac{1}{q} = \frac{p+q}{pq}$	M1
	$\frac{p+q}{pq} = \frac{p+q}{\frac{5}{2}} = \frac{4}{5} \Rightarrow p+q = \frac{4}{5} \times \frac{5}{2} = 2$	" $p+q=2$ " from correct work. Allow " $2 = q+p$ "	A1
(4)			
Alt $x \rightarrow \frac{1}{z}$	$x \rightarrow \frac{1}{z} \Rightarrow 5\left(\frac{1}{z}\right)^2 - 4\left(\frac{1}{z}\right) + 2 = 0$	Correctly replaces x with e.g., $\frac{1}{z}$ and allow $\frac{1}{x}$	1st M1
	$2z^2 - 4z + 5 = 0$	Obtains a 3TQ in "z", "w" etc.	2nd M1
	$pq = \frac{5}{2}$	States $pq = \frac{5}{2}$ following correct work	B1* 1st mark
	$p+q=2$	" $p+q=2$ " from correct work	A1

Question Number	Scheme	Notes	Marks
5(b)	$\frac{p}{p^2+1} + \frac{q}{q^2+1} = \frac{pq^2 + p + p^2q + q}{p^2q^2 + p^2 + q^2 + 1}$ $\frac{p}{p^2+1} \times \frac{q}{q^2+1} = \frac{pq}{p^2q^2 + p^2 + q^2 + 1}$ <p>M1: For $p(q^2+1) + q(p^2+1) \rightarrow pq^2 + p + p^2q + q$ or $(p^2+1)(q^2+1) \rightarrow p^2q^2 + p^2 + q^2 + 1$</p> <p>Allow equivalents e.g., $pq(p+q) + p + q$ provided the initial expansion has been carried out</p> <p>A1: Both correct (expression for denominator seen correctly once)</p> <p>Do not accept pq^2 for $(pq)^2$ unless it is clearly recovered</p>		M1 A1
	$\text{sum} = \frac{pq(p+q) + p + q}{(pq)^2 + (p+q)^2 - 2pq + 1} = \frac{\frac{5}{2} \times 2 + 2}{(\frac{5}{2})^2 + 2^2 - 2 \times \frac{5}{2} + 1} = \frac{7}{\frac{25}{4}} = \dots \left(\frac{28}{25} \text{ or } 1.12 \right)$ $\text{product} = \frac{pq}{(pq)^2 + (p+q)^2 - 2pq + 1} = \frac{\frac{5}{2}}{(\frac{5}{2})^2 + 2^2 - 2(\frac{5}{2}) + 1} = \frac{\frac{5}{2}}{\frac{25}{4}} = \dots \left(\frac{2}{5} \text{ or } 0.4 \right)$ <p>Obtains a value for either the new sum or new product using $pq = \frac{5}{2}$ and a value for $p+q$</p> <p>which could be their answer from part (a)(ii) and may have been stated as e.g., $\frac{1}{p} + \frac{1}{q}$ or it could be inconsistent with their answer to (a)(ii). May be slips.</p> <p>At least one of their expressions must have included both pq and $p+q$ and have been completely in terms of pq and $p+q$ including at least one use of $p^2 + q^2 = (p+q)^2 - 2pq$.</p> <p>Accept just sum = $\frac{28}{25}$ or product = $\frac{2}{5}$ if there is no clearly incorrect work otherwise some evidence of all of the above conditions and not just values must be seen.</p> <p>Requires previous M mark.</p>		dM1
	<p>Note that for the numerator of the sum it is possible to use</p> $pq^2 + p + p^2q + q = p + q + (p+q)(p^2 + q^2) - (p^3 + q^3) = p + q + (p+q)((p+q)^2 - 2pq) - ((p+q)^3 - 3pq(p+q))$ <p>in which case both $p^2 + q^2 = (p+q)^2 - 2pq$ and $p^3 + q^3 = (p+q)^3 - 3pq(p+q)$ must be used</p>		
	The above work may be embedded within $x^2 \pm (\text{sum})x \pm \text{product}$		
	$x^2 - \frac{28}{25}x + \frac{2}{5}$	Applies $x^2 - (\text{sum})x + \text{product}$ correctly for their stated values for new sum and product. Not dependent.	M1
	$25x^2 - 28x + 10 = 0$	Correct quadratic (or integer multiple) with “= 0” Allow a different variable e.g., z for x Allow e.g., $a = 25, b = -28, c = 10$ provided $ax^2 + bx + c = 0$ is seen otherwise score M1A0	A1
(5)			
Total 9			

Question Number	Scheme	Notes	Marks
6(a)	$\begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^n = \begin{pmatrix} 1 & (2^n - 1)r \\ 0 & 2^n \end{pmatrix}$		
	Evaluates LHS & RHS for $n = 1$. LHS & RHS indicated (or “true” seen) if not equated $(\text{LHS}) = \begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^1 \text{ or } \begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} 1 & (2^1 - 1)r \\ 0 & 2^1 \end{pmatrix} \text{ or } \begin{pmatrix} 1 & (2 - 1)r \\ 0 & 2 \end{pmatrix} (= \text{RHS})$		B1
	Assume true for $n = k$, i.e., $\begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^k = \begin{pmatrix} 1 & (2^k - 1)r \\ 0 & 2^k \end{pmatrix}$		
	$\begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^{k+1} = \begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 1 & (2^k - 1)r \\ 0 & 2^k \end{pmatrix}$	Uses $n = k$ result to form expression for $\begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^{k+1}$ Implied by 3 correct elements if they immediately multiply provided the result is not just the “given” answer and allow this to be the intermediate step	M1
	$= \begin{pmatrix} 1 & (2^k - 1)r + 2^k r \\ 0 & 2(2^k) \end{pmatrix} = \begin{pmatrix} 1 & (2^{k+1} - 1)r \\ 0 & 2^{k+1} \end{pmatrix}$	Correct result with intermediate step that involves the top right element and no errors seen in the algebra. Allow “meet in the middle” proofs. Only allow $(2^{k+1} - 1)r$ written as $r(2^{k+1} - 1)$ or $(-1 + 2^{k+1})r$ or $r(-1 + 2^{k+1})$. No $2(2^k)$ s for 2^{k+1}	A1
	Alternatively: $\begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix}^{k+1} = \begin{pmatrix} 1 & (2^k - 1)r \\ 0 & 2^k \end{pmatrix} \begin{pmatrix} 1 & r \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} 1 & r + 2(2^k - 1)r \\ 0 & 2(2^k) \end{pmatrix} = \begin{pmatrix} 1 & (2^{k+1} - 1)r \\ 0 & 2^{k+1} \end{pmatrix}$		
<p>True for $n = 1$, if true for $n = k$ then true for $n = k + 1$, true for all (positive integers) n Correct conclusion or narrative. Minimum in bold. “Assume true for $n = k$... true for $n = k + 1$” is sufficient for the “then” The two previous marks are required and this mark can only follow B0 if the B mark was only withheld for insufficient working provided there was an attempt with $n = 1$. Ignore further verifications for $n = 2$ etc. Condone “for all $n \in \mathbb{Z}$” but not $n \in \mathbb{R}$ Condone work with n used for k.</p>			A1
(4)			
(b)(i)	$\begin{pmatrix} 1 & -2 \\ 0 & 2 \end{pmatrix}^4 = \begin{pmatrix} 1 & (2^4 - 1)(-2) \\ 0 & 2^4 \end{pmatrix} = \begin{pmatrix} 1 & -30 \\ 0 & 16 \end{pmatrix}$	Correct matrix N . Could come from manual multiplication or calculator	B1
(ii)	$\mathbf{B} = \mathbf{NM} = \begin{pmatrix} 1 & -30 \\ 0 & 16 \end{pmatrix} \begin{pmatrix} 4 & 0 \\ 0 & 5 \end{pmatrix} = \dots$	Attempts NM with their N . Must not be MN . The N must have exactly three non-zero elements with 0 as the first element in the second row and their NM must have three elements correct for their matrices	M1
	$\begin{pmatrix} 4 & -150 \\ 0 & 80 \end{pmatrix}$	Correct matrix B	A1
(3)			
(c)	$\det \mathbf{B} = 4 \times 80 - (0 \times (-150)) = 320$ area $S = \frac{720}{320}$	A correct non-zero value for the determinant of their B (no more than two zero elements) and divides this result into 720 to obtain a value for the area	M1
	$\frac{9}{4}$ or $2\frac{1}{4}$ or 2.25	Correct area. Any exact equivalent. <u>Must follow a correct B</u> . Answer only is M1A1 if B correct.	A1
(2)			
Total 9			

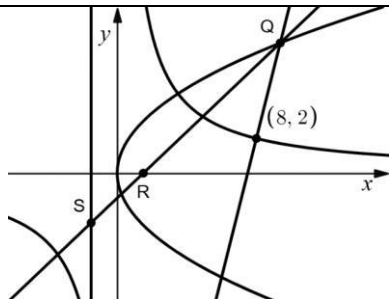
Question Number	Scheme	Notes	Marks
7(a)	$\sum_{r=1}^n (12r^2 + 2r - 3) = 12 \sum_{r=1}^n r^2 + 2 \sum_{r=1}^n r - 3 \sum_{r=1}^n 1$ $= 12 \times \frac{n}{6} (n+1)(2n+1) + 2 \times \frac{n}{2} (n+1) - 3n$ $[= 2n(n+1)(2n+1) + n(n+1) - 3n]$	<p>M1: Expands summation to at least 2 separate sums with one correct (could be implied), uses $\sum_{r=1}^n r^2 = \frac{n}{6} (n+1)(2n+1)$ (allowing one of the following slips within the formula above: One of the 2 + signs seen as – or a missing first n) and replaces $\sum_{r=1}^n r$ with $\frac{n}{2} (n+1)$ or $\sum_{r=1}^n 1$ with n Condone r used for n for the first three marks only. Allow \sum for $\sum_{r=1}^n$ A1: Fully correct unsimplified expression</p>	M1 A1
	$\sum_{r=1}^n (12r^2 + 2r - 3) = 4n^3 + 6n^2 + 2n + n^2 + n - 3n = \dots$	<p>Expands to a cubic and collects terms. Allow slips. Requires previous M mark.</p>	dM1
	$4n^3 + 7n^2$	<p>Correct expression from correct work Allow $A = 4, B = 7$ following "$= An^3 + Bn^2$"</p>	A1
	(4)		
(b)	Full marks in (b) does not require full marks in (a)		
	$\sum_{r=1}^{2n} r^3 = \frac{(2n)^2}{4} (2n+1)^2$	<p>Attempts to use the sum of cubes formula with $2n$ Allow one of the following two slips: $2n^2$ for $(2n)^2$ Only one of the n's in the formula replaced by $2n$</p>	M1
	$\sum_{r=1}^{2n} r^3 - \sum_{r=1}^n (12r^2 + 2r - 3) =$ $4n^4 + 4n^3 + n^2 - "4"n^3 - "7"n^2 [= 270]$ $[\Rightarrow 4n^4 - 6n^2 = 270]$	<p>Correct expanded quartic expression for $\sum_{r=1}^{2n} r^3 - \sum_{r=1}^n (12r^2 + 2r - 3)$ (ft their $An^3 + Bn^2$) No requirement to collect terms but must be correct for their A and B if expression only seen with terms collected. If this is only seen as an equation it must be correct.</p>	A1ft
	$4n^4 - 6n^2 - 270 = 0 \Rightarrow$ $2n^4 - 3n^2 - 135 = (2n^2 + 15)(n^2 - 9) = 0$ $\Rightarrow n^2 = \dots$	<p>Solves their 3TQ in n^2 (usual rules and allow for one correct root if no working). May change variable e.g., $n^2 \rightarrow x$ Ignore the labelling of roots (e.g. "$n = \dots$") Allow for solving as a quartic if one root correct but requires $pn^4 + qn^2 + r = 0$ oe, $p, q, r \neq 0$ Requires previous M mark.</p>	dM1
	$n^2 = 9 \Rightarrow n = 3$	<p>$n = 3$ and no other unrejected solutions. $n = \pm 3$ is A0 Must follow a correct equation.</p>	A1
(4)			
Total 8			

Question Number	Scheme	Notes	Marks
8	$f(k) = 7^{k-1} + 8^{2k+1}$		
	<p>General guidance:</p> <p>Apply the Way that best fits the overall approach.</p> <p>Condone work in e.g., n instead of k.</p> <p>Allow use of -57 but if any different multiples of 57 are involved, e.g., 114, the last A1 additionally requires “114 is a multiple of/divisible by (but not “factor of”) 57” oe for each case. Ignore work re the divisibility of $f(2)$, $f(3)$ etc but starting with e.g., $f(2)$ scores a max of 01110.</p> <p>Final A1: There must be evidence that true for $n = k \Rightarrow$ true for $n = k + 1$ but it could be minimal and be scored in a conclusion or a narrative or via both. So if e.g., “Assume true for $n = k \dots$” is seen in the work followed by “true for $n = k + 1$” in a conclusion this is sufficient. May say “is divisible by 57” for “true”. Condone “for all $n \in \mathbb{Z}$” but not $n \in \mathbb{R}$</p>		
Way 1 $f(k+1)$ $-f(k)$	$n = 1: f(1) = [7^0 + 8^3 =] 513,$ $513 \div 57 = 9$ oe	Obtains 513 for $f(1)$ and shows 513 is divisible by 57. Allow $\frac{1+512}{57} = 9$	B1
	$[f(k+1) =] 7^{(k+1)-1} + 8^{2(k+1)+1} \{ = 7^k + 8^{2k+3} \}$	Attempts $f(k+1)$	M1
	$[f(k+1) - f(k) =]$ $7(7^{k-1}) - 7^{k-1} + 8^2(8^{2k+1}) - 8^{2k+1}$	Obtains expression for $f(k+1) - f(k)$ in 7^{k-1} and 8^{2k+1} only	M1
	$= 6(7^{k-1} + 8^{2k+1}) + 57(8^{2k+1})$ $\Rightarrow f(k+1) = 7f(k) + 57(8^{2k+1})$ or $= 63(7^{k-1} + 8^{2k+1}) - 57(7^{k-1})$ $\Rightarrow f(k+1) = 64f(k) - 57(7^{k-1})$	M1: Obtains expression for $f(k+1)$ in terms of $f(k)$. May not see $f(k+1) = \dots$ A1: Correct expression. Must see $f(k+1) = \dots$ Allow if e.g., $7f(k)$ written as $7(7^{k-1} + 8^{2k+1})$ or $7(7^{k-1}) + 7(8^{2k+1})$	M1 A1
	Shown true for $n = 1$ and if true for $n = k$ then true for $n = k + 1$ so true for all n ($\in \mathbb{Z}^+$)	Makes correct conclusion or narrative with no errors throughout. Minimum in bold . Requires all previous marks but can follow B0 if that mark was withheld for omitting to show that 513 is divisible by 57.	A1
(6)			
Way 2 $f(k+1) =$	$n = 1: f(1) = [7^0 + 8^3 =] 513,$ $513 \div 57 = 9$ oe	Obtains 513 for $f(1)$ and shows 513 is divisible by 57. Allow $\frac{1+512}{57} = 9$	B1
	$[f(k+1) =] 7^{(k+1)-1} + 8^{2(k+1)+1} \{ = 7^k + 8^{2k+3} \}$	Attempts $f(k+1)$	M1
	$[f(k+1) =] 7(7^{k-1}) + 8^2(8^{2k+1})$	Obtains expression for $f(k+1)$ in 7^{k-1} and 8^{2k+1} only	M1
	$= 7(7^{k-1} + 8^{2k+1}) + 57(8^{2k+1})$ $\Rightarrow f(k+1) = 7f(k) + 57(8^{2k+1})$ or $= 64(7^{k-1} + 8^{2k+1}) - 57(7^{k-1})$ $\Rightarrow f(k+1) = 64f(k) - 57(7^{k-1})$	M1: Obtains expression for $f(k+1)$ in terms of $f(k)$. May not see $f(k+1) = \dots$ A1: Correct expression. Must see $f(k+1) = \dots$ Allow if e.g., $7f(k)$ written as $7(7^{k-1} + 8^{2k+1})$ or $7(7^{k-1}) + 7(8^{2k+1})$	M1 A1
	Shown true for $n = 1$ and if true for $n = k$ then true for $n = k + 1$ so true for all n ($\in \mathbb{Z}^+$)	Makes correct conclusion or narrative with no errors throughout. Minimum in bold . Requires all previous marks but can follow B0 if that mark was withheld for omitting to show that 513 is divisible by 57.	A1
(6)			

Question Number	Scheme	Notes	Marks
8 Way 3 $f(k+1) - mf(k)$	$n = 1: f(1) = [7^0 + 8^3 =] 513,$ $513 \div 57 = 9$ oe	Obtains 513 for $f(1)$ and shows 513 is divisible by 57. Allow $\frac{1+512}{57} = 9$	B1
	$[f(k+1) =] 7^{(k+1)-1} + 8^{2(k+1)+1} \{ = 7^k + 8^{2k+3} \}$	Attempts $f(k+1)$	M1
	$f(k+1) - mf(k)$ $= 7(7^{k-1}) - (7^{k-1})m + 8^2(8^{2k+1}) - (8^{2k+1})m$	Obtains expression for $f(k+1) - mf(k)$ in 7^{k-1} and 8^{2k+1} only	M1
	e.g., $m = 7 \Rightarrow$ $f(k+1) - 7f(k) = 57(8^{2k+1})$ $\Rightarrow f(k+1) = 7f(k) + 57(8^{2k+1})$ e.g., $m = 64 \Rightarrow$ $f(k+1) - 64f(k) = -57(7^{k-1})$ $\Rightarrow f(k+1) = 64f(k) - 57(7^{k-1})$	M1: Obtains expression for $f(k+1)$ in terms of $f(k)$ using a value for m . May not see $f(k+1) = \dots$ A1: A correct expression. Must see $f(k+1) = \dots$ Allow if $\beta f(k)$ written as $\beta(7^{k-1} + 8^{2k+1})$ or $\beta(7^{k-1}) + \beta(8^{2k+1})$	M1 A1
	Shown true for $n = 1$ and if true for $n = k$ then true for $n = k + 1$ so true for all n ($\in \mathbb{Z}^+$)	Makes correct conclusion or narrative with no errors throughout. Minimum in bold . Requires all previous marks but can follow B0 if that mark was withheld for omitting to show that 513 is divisible by 57.	A1
(6)			
Way 4 $f(k) = 57\lambda$	$n = 1: f(1) = [7^0 + 8^3 =] 513,$ $513 \div 57 = 9$ oe	Obtains 513 for $f(1)$ and shows 513 is divisible by 57. Allow $\frac{1+512}{57} = 9$	B1
	$[f(k+1) =] 7^{(k+1)-1} + 8^{2(k+1)+1} \{ = 7^k + 8^{2k+3} \}$	Attempts $f(k+1)$	M1
	$[f(k+1) =] 7(7^{k-1}) + 8^2(8^{2k+1})$	Obtains expression for $f(k+1)$ in 7^{k-1} and 8^{2k+1} only	M1
	$= 7(7^{k-1} + 8^{2k+1}) + 57(8^{2k+1})$ $f(k) = 57\lambda \Rightarrow f(k+1) = 399\lambda + 57(8^{2k+1})$ or $= 7 \times 57\lambda + 57(8^{2k+1})$ or $= 64(7^{k-1} + 8^{2k+1}) - 57(7^{k-1})$ $f(k) = 57\lambda \Rightarrow f(k+1) = 64 \times 57\lambda - 57(7^{k-1})$ or $= 3648\lambda - 57(7^{k-1})$	M1: Obtains expression for $f(k+1)$ in terms of λ with $f(k) = 57\lambda$ seen. May not see $f(k+1) = \dots$ A1: Correct expression Must see $f(k+1) = \dots$	M1 A1
	Shown true for $n = 1$ and if true for $n = k$ then true for $n = k + 1$ so true for all n ($\in \mathbb{Z}^+$)	Makes correct conclusion or narrative with no errors throughout. Minimum in bold . Requires all previous marks but can follow B0 if that mark was withheld for omitting to show that 513 is divisible by 57.	A1
(6)			
Total 6			

Question Number	Scheme	Notes	Marks
9(a)	$y = c^2 x^{-1}$ $\frac{dy}{dx} = -c^2 x^{-2} = -\frac{c^2}{x^2}$ $\left(ct, \frac{c}{t}\right) \Rightarrow \frac{dy}{dx} = -\frac{c^2}{c^2 t^2}$ <p>Correct expression for $\frac{dy}{dx}$ in terms of c and t (or just t). Award when seen and isw.</p> <p>Allow for a correct $\frac{dx}{dy}$ or $-\frac{dx}{dy}$</p>	$xy = c^2$ $y + x \frac{dy}{dx} = 0$ $\frac{dy}{dx} = -\frac{y}{x} \Rightarrow \frac{-\frac{c}{t}}{ct}$ $x = ct \quad y = \frac{c}{t}$ $\frac{dx}{dt} = c \quad \frac{dy}{dt} = -ct^{-2}$ $\frac{dy}{dx} = -\frac{ct^{-2}}{c}$	B1
	$m_T = -\frac{1}{t^2} \Rightarrow m_N = t^2$	Correct perpendicular gradient rule for their $\frac{dy}{dx}$ in terms of t (or c and t)	M1
	$y - \frac{c}{t} = "t^2"(x - ct) \quad \text{or}$ $y = "t^2" x + b \Rightarrow \frac{c}{t} = "t^2"(ct) + b \Rightarrow b = \dots$	Correct straight line method with a changed gradient in terms of t (or c and t) with coordinates correctly placed. Condone the use of $y = mx + c$ instead of e.g. $y = mx + b$	M1
	$ty - c = t^3 x - ct^4 \quad \text{or} \quad y = t^2 x + \frac{c}{t} - ct^3$ $\Rightarrow t^3 x - ty = c(t^4 - 1)^*$	Fully correct proof with at least one intermediate line before printed answer but allow if equation reversed and/or order altered e.g., $(-1 + t^4)c = -ty + t^3 x$	A1*
	Score a maximum of 0110 if they start with just $\frac{dy}{dx} = -\frac{1}{t^2}$ and 0010 if just $m_N = t^2$		
(4)			

Question Number	Scheme	Notes	Marks
9(b)	$(8, 2) \Rightarrow \text{e.g., } c^2 = 16, c = 4;$ $ct = 8 \text{ or } \frac{c}{t} = 2 \Rightarrow t = 2$	Correct values for c and t seen, used or implied (e.g., by correct normal). If $c = \pm 4, t = \pm 2$ then the positive values must be implied by subsequent work	B1
	Note that another way of finding t is by using $c = 4$ and $(8, 2)$ in the normal: $\Rightarrow 8t^3 - 2t = 4(t^4 - 1) \Rightarrow 4t^4 - 8t^3 + 2t - 4 = (t - 2)(4t^3 + 2) = 0 \Rightarrow t = 2$		
	normal : $8x - 2y = 60 \Rightarrow$ $y = 4x - 30 \text{ or } x = \frac{15}{2} + \frac{1}{4}y$ $\Rightarrow (4x - 30)^2 = 6x \text{ or } y^2 = 45 + \frac{3}{2}y$	Uses their values of c and t in the given normal $t^3x - ty = c(t^4 - 1)$ [could repeat the work in (a) with $y = 16x^{-1}$] and substitutes into the parabola to obtain a quadratic equation. Note that appropriate work must be seen for this mark. $4x - 30 = \sqrt{6x}$ must be followed by a credible attempt to square (i.e., a 3TQ on LHS and ... x on the RHS) but see note below	M1
	Note that replacing x with e.g., k^2 in $4x - 30 = \sqrt{6x} \rightarrow$ $4k^2 - 30 = \sqrt{6}k \Rightarrow k = \frac{\sqrt{6} \pm \sqrt{6 - 4(4)(-30)}}{2(4)} = \frac{5\sqrt{6}}{4}, -\sqrt{6} \Rightarrow x = \frac{75}{8}, 6$ Scores the M1 for the quadratic in k and the dM1 for solving via usual rules and also reaching $x = \dots$ by squaring.		
	$16x^2 - 246x + 900 = 0 \Rightarrow 8x^2 - 123x + 450 = 0$ $\Rightarrow (8x - 75)(x - 6) = 0 \Rightarrow x = \dots \text{ or }$ $2y^2 - 3y - 90 = 0 \Rightarrow (2y - 15)(y + 6) = 0 \Rightarrow y = \dots$	Solves 3TQ (usual rules – one correct root if no working). Requires previous method mark.	dM1
	$x = \frac{75}{8}, y = \frac{15}{2} \text{ or e.g., } Q(9.375, 7.5)$	Correct values/coordinates. Allow any equivalent fractions. If a second point is given e.g., $(6, -6)$ or $(6, 6)$ score A0 if it is not rejected in (b).	A1
(4)			
Alt Approaches using parametric coords	$c = 4, t = 2$	Correct values for c and t seen or used	B1
	Let Q have coordinates $(\frac{3}{2}k^2, 3k)$: Substituting into the normal with $c = 4$ and $t = 2$: $8(\frac{3}{2}k^2) - 2(3k) = 4(16 - 1)$ OR Since gradient of normal to hyperbola $= t^2 = 4$, gradient of AQ where A is $(8, 2) = \frac{3k - 2}{\frac{3}{2}k^2 - 8} = 4$ Forms a quadratic equation with their values. The equation in case 2 implies the B1.		M1
	$12k^2 - 6k = 60$ or $3k - 2 = 6k^2 - 32 \Rightarrow 6k^2 - 3k - 30 = 0$ $\Rightarrow 2k^2 - k - 10 = 0 \Rightarrow (2k - 5)(k + 2) = 0 \Rightarrow k = \dots[\frac{5}{2}]$ $\Rightarrow x = \dots \text{ or } y = \dots$	Solves 3TQ (usual rules – one correct root if no working) and proceeds to a value of x or y Requires previous method mark.	dM1
	$x = \frac{75}{8}, y = \frac{15}{2} \text{ or e.g., } Q(9\frac{3}{8}, 7\frac{1}{2})$	Correct values/coordinates. Allow any equivalent fractions. If a second point is given e.g., $(6, -6)$ or $(6, 6)$ score A0 if it is not rejected in (b).	A1
(4)			

Question Number	Scheme	Notes	Marks
9(c)	$R\left(\frac{3}{2}, 0\right)$ Correct coordinates for the focus seen or used. Can score anywhere e.g., written across the question. Condone sight of $\left(0, \frac{3}{2}\right)$ if used correctly e.g. in gradient calculation. If on a diagram, accept $\frac{3}{2}$ appropriately placed. Accept 1.5, $\frac{6}{4}$ etc. for $\frac{3}{2}$. Just " a or $x = \frac{3}{2}$ " or " $R = \frac{3}{2}$ " is insufficient. There must be some recognition of the <u>position</u> of R .		B1
	Allow work with decimals for the 3 M marks.		
	QR : e.g., $y - 0 = \left(\frac{\frac{15}{2} - 0}{\frac{75}{8} - \frac{3}{2}}\right)(x - \frac{3}{2})$ or $y = \left(\frac{\frac{15}{2} - 0}{\frac{75}{8} - \frac{3}{2}}\right)x + c \Rightarrow 0 = \frac{20}{21}\left(\frac{3}{2}\right) + c \Rightarrow c = \dots$ Correctly forms equation of QR for their Q and R . Q could be "made up" or be an incorrect choice from part (b) but must have real coordinates (A, B) , $A > 0$, $B \neq 0$ so allow e.g., (6, 6) and (6, -6). R must be of form $(\alpha, 0)$, $\alpha > 0$ Allow if a correct gradient is seen but wrongly calculated before line equation is given. If using $y = mx + c$ the equation must be formed correctly and " $c = \dots$ " reached following correct placement of $(\alpha, 0)$. For $0 = \frac{3}{2}m + c$, $\frac{15}{2} = \frac{75}{8}m + c \Rightarrow m = \dots$, $c = \dots$ must find both m and c with one correct M0 for a vertical line or if a normal gradient is used		M1
	$y = \frac{20}{21}x - \frac{10}{7}$, $x = -\frac{3}{2}$ $\Rightarrow y = \frac{20}{21}\left(-\frac{3}{2}\right) - \frac{10}{7} = -\frac{10}{7} - \frac{10}{7} = -\frac{20}{7}$	Substitutes $x = -\alpha$, $\alpha > 0$ into their equation to find a value for the y coordinate. Must be using a consistent α Requires previous M mark.	
	$S\left(-\frac{3}{2}, -\frac{20}{7}\right) \Rightarrow$ $QS = \sqrt{\left(\frac{75}{8} - \left(-\frac{3}{2}\right)\right)^2 + \left(\frac{15}{2} - \left(-\frac{20}{7}\right)\right)^2}$	Applies correct distance formula for their $Q(A, B)$, $A > 0$, $B \neq 0$ and $S(-\alpha, \pm\beta)$ $\alpha > 0$ and consistent, $\beta \neq 0$ Implied by 15.017857... otherwise working must be seen. Requires both previous M marks. Note that using (6, 6) or (6, -6) $\rightarrow QS = \frac{25}{2}$	ddM1
	$\left[= \sqrt{\left(\frac{87}{8}\right)^2 + \left(\frac{145}{14}\right)^2} = \sqrt{\frac{7569}{64} + \frac{21025}{196}} = \sqrt{\frac{707281}{3136}} = \right] \Rightarrow QS = \frac{841}{56}$ Correct exact distance. Any exact equivalent e.g., $15\frac{1}{56}$ and may not be in simplest form		A1
Alt For the last two marks ($QS = QR + RS$)	$QS = QR + RS$ but QR = shortest distance of Q to directrix $= \frac{75}{8} + \frac{3}{2} = \frac{87}{8}$ $QS = \sqrt{\left(0 - \left(-\frac{20}{7}\right)\right)^2 + \left(\frac{3}{2} - \left(-\frac{3}{2}\right)\right)^2} + \frac{87}{8} = \frac{29}{7} + \frac{87}{8} = \frac{841}{56}$ M1: A full method correct for their Q and S . Implied only by awrt 15.017857... A1: Correct exact distance (any equivalent)		
			
(5)			
Total 13			
PAPER TOTAL: 75 marks			